

TSTE26 Powergrid and technology for renewable
production

Lecture 7

Converter control

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ICS/ISY

Outline

- Grid inverter
 - Power control
 - Current control
- Coordinate transforms
 - DQ-frame
- Phase Locked Loop
- PV with MPPT + Grid inverter (Lab3)

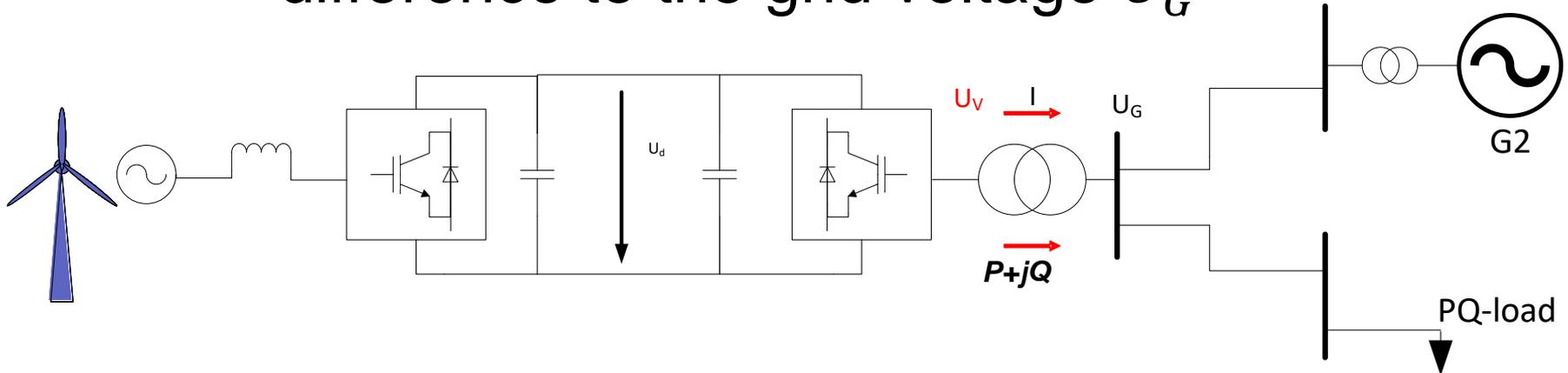
Grid Converters for Photovoltaic and Wind Power Systems by Remus Teodorescu, Marco Liserre, Pedro Rodriguez

Chapter 4.2.2 Grid synchronization using PLL

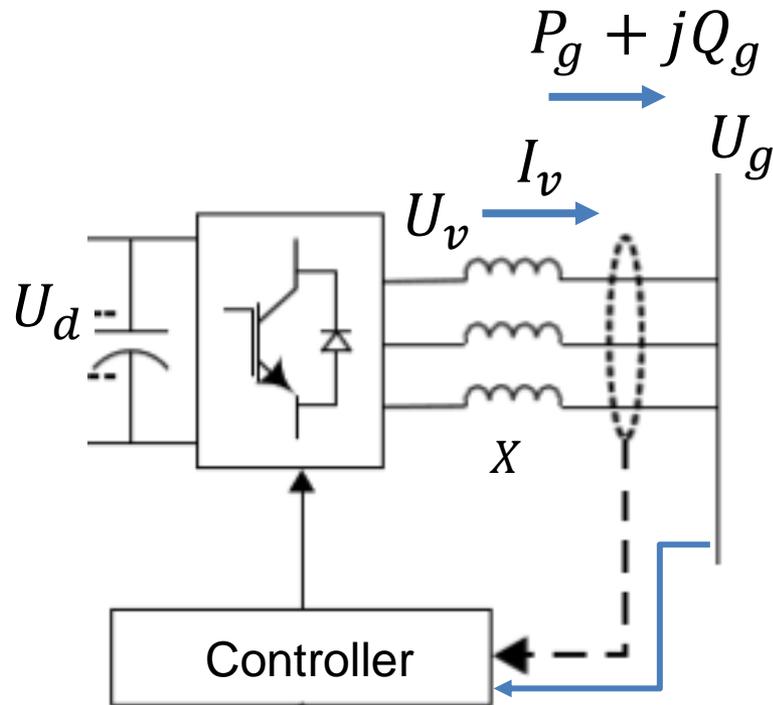
Appendix A: Space Vector Transformations of Three-Phase Systems

Grid power infeed

- Converter infeed of $P + jQ$ through the current injection I by controlling \bar{U}_v
- $\bar{U}_v = U_v \angle \delta$, where δ is the angle difference to the grid voltage \bar{U}_G



VSC power flow control



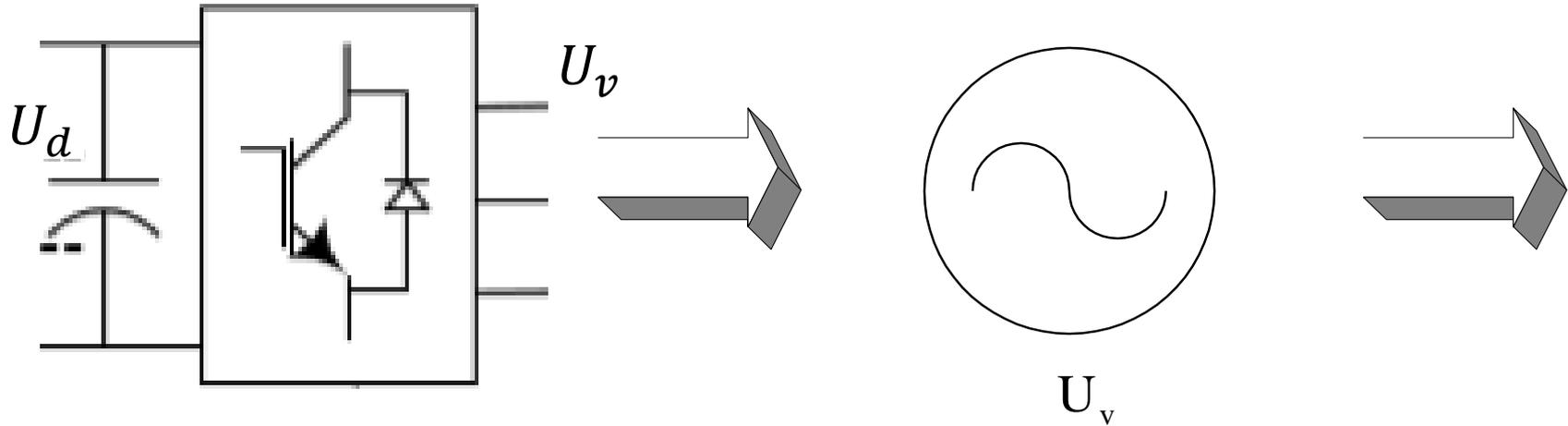
$$\bar{I}_v = \frac{U_v \angle \delta - U_g}{jX\sqrt{3}}$$

Note $\sqrt{3}$ in the denominator since the voltages are ph-ph

$$P_g + jQ_g = \sqrt{3} \cdot U_g \cdot \bar{I}_v^*$$

- The converter ph-ph rms voltage U_v
- δ the angle difference between U_v and U_g

Voltage Source Converter (VSC)



U_v adjustable

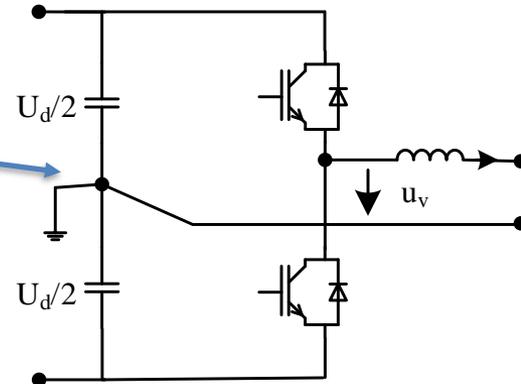
{ amplitude
phase angle
frequency

Half-bridge (2-level) converter

- DC-side midpoint reference point for ac-output
- Output voltage, u_v , switched between $+\frac{U_d}{2}$ and $-\frac{U_d}{2}$
- Output peak phase voltage defined by modulation index

m_a

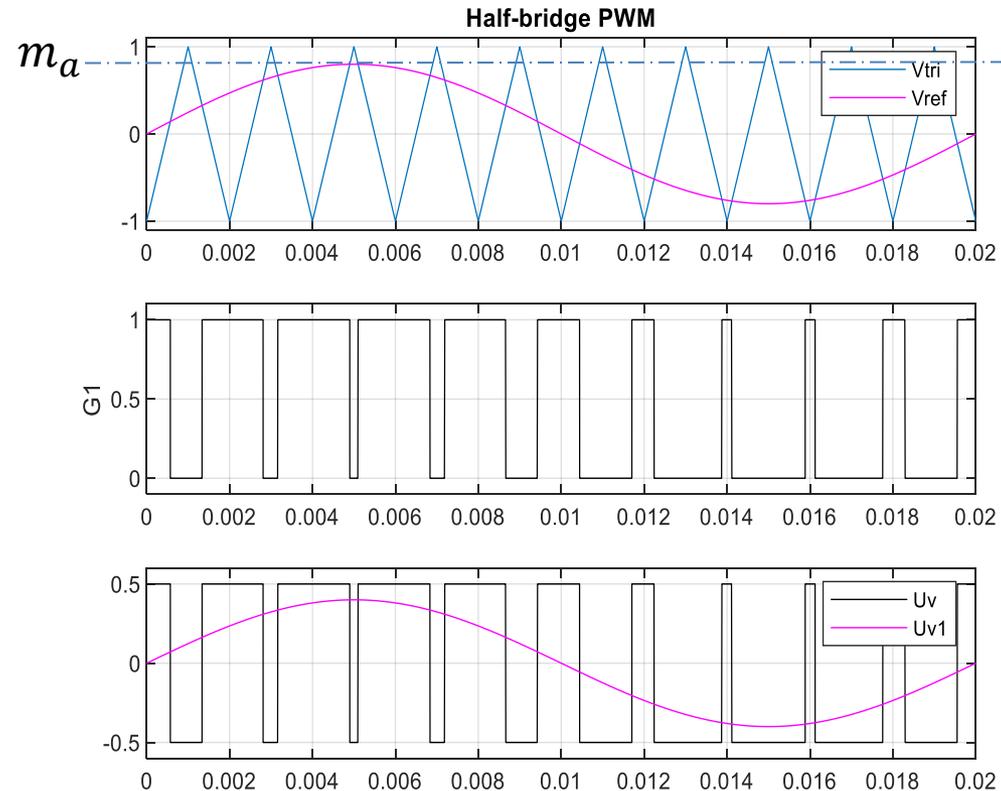
$$\hat{u}_{v1} = m_a \frac{U_d}{2}$$



Pulse-width modulated (PWM) switching scheme

- Constant switching frequency (triangle wave) f_s
- Amplitude modulation ratio

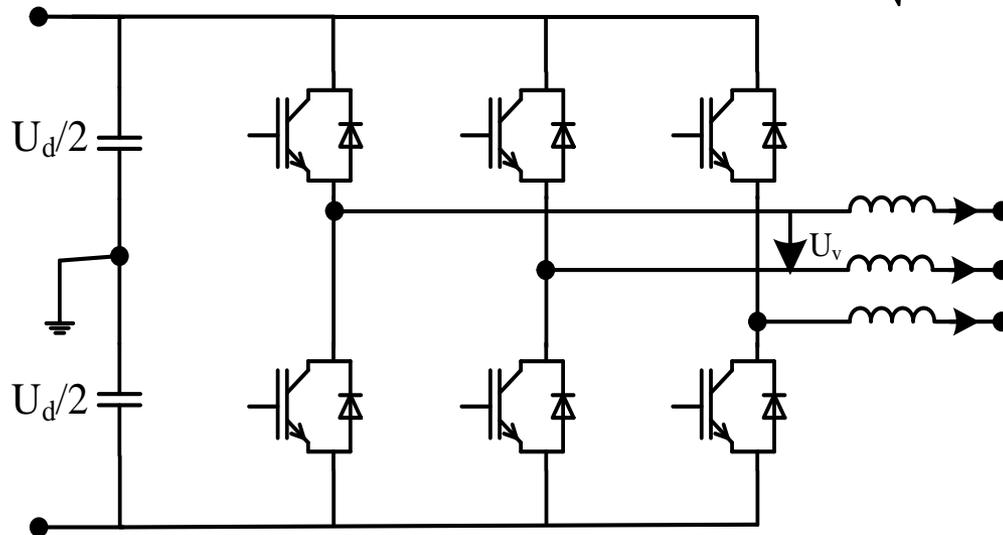
$$m_a = \frac{\hat{U}_v}{U_d/2} = \frac{\hat{U}_{v_ref}}{\hat{U}_{tri}}$$



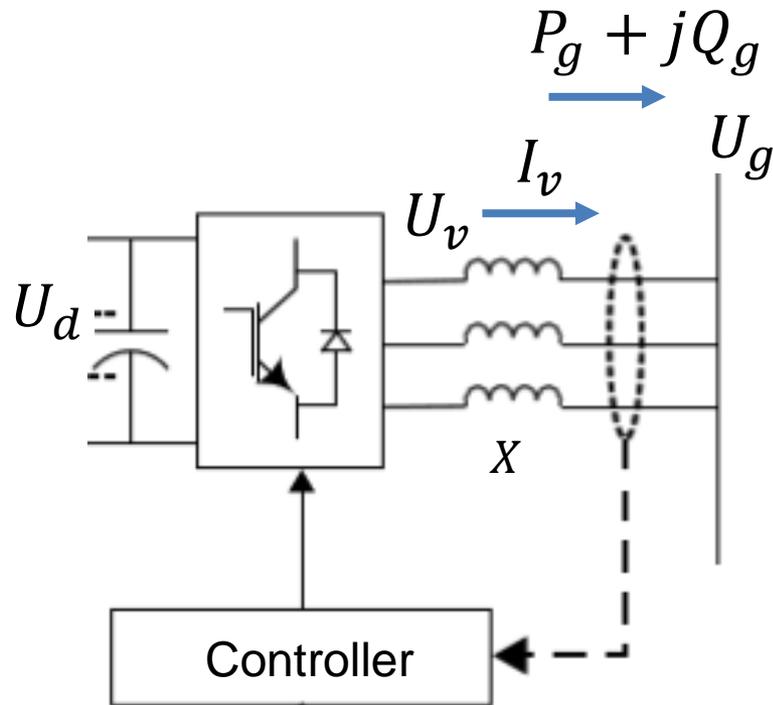
Three-phase inverters

- Three legs
- Controls phase shifted 120°
- Midpoint not used
- Output ph-ph rms voltage

$$U_v = \sqrt{\frac{3}{2}} \cdot m_a \frac{U_d}{2}$$



VSC power flow control



$$\bar{I}_v = \frac{U_v \angle \delta - U_g}{jX\sqrt{3}}$$

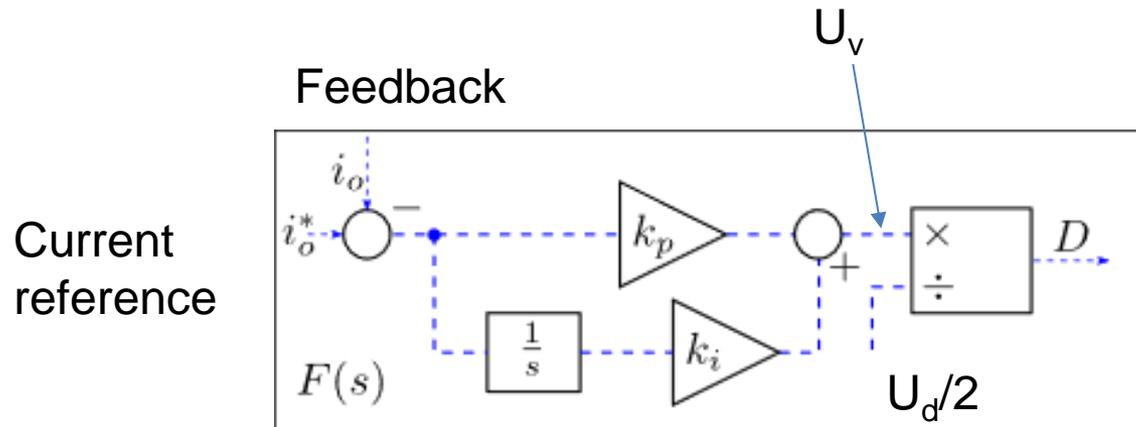
Note $\sqrt{3}$ in the denominator since the voltages are ph-ph

$$P_g + jQ_g = \sqrt{3} \cdot U_g \cdot \bar{I}_v^*$$

- The converter ph-ph rms voltage U_v

$$U_v = \sqrt{\frac{3}{2}} \cdot m_a \frac{U_d}{2}$$

PI-control



Load angle control of P and Q

- Active power $\sim \sin \delta$
- Reactive power $\sim V_S - V_R$

$$P_R = \frac{V_S V_R}{X} \sin \delta$$

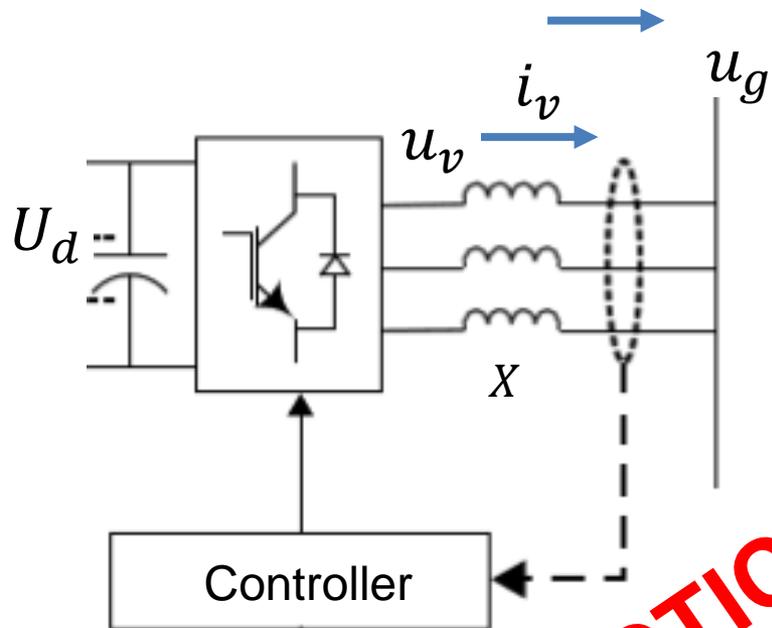
$$Q_R = \frac{V_S V_R \cos \delta}{X} - \frac{V_R^2}{X}$$

P and Q not independent

- Q also depend on δ
- P also depend on $V_S V_R$

Current control in abc-frame

$$P_g + jQ_g = 3 \cdot u_g \cdot i_v$$



- u_v is controlled to achieve $i_v = i_{vRef}$

- u_g and i_v are measured

- $u_v = u_g + L \frac{di_v}{dt}$

- Each phase controlled separately

- PI-control not practical due to sinusoidal reference

- $i_{vRef} = \hat{I}_{vRef} \cos(\omega t + \varphi)$

Three-Phase Voltages

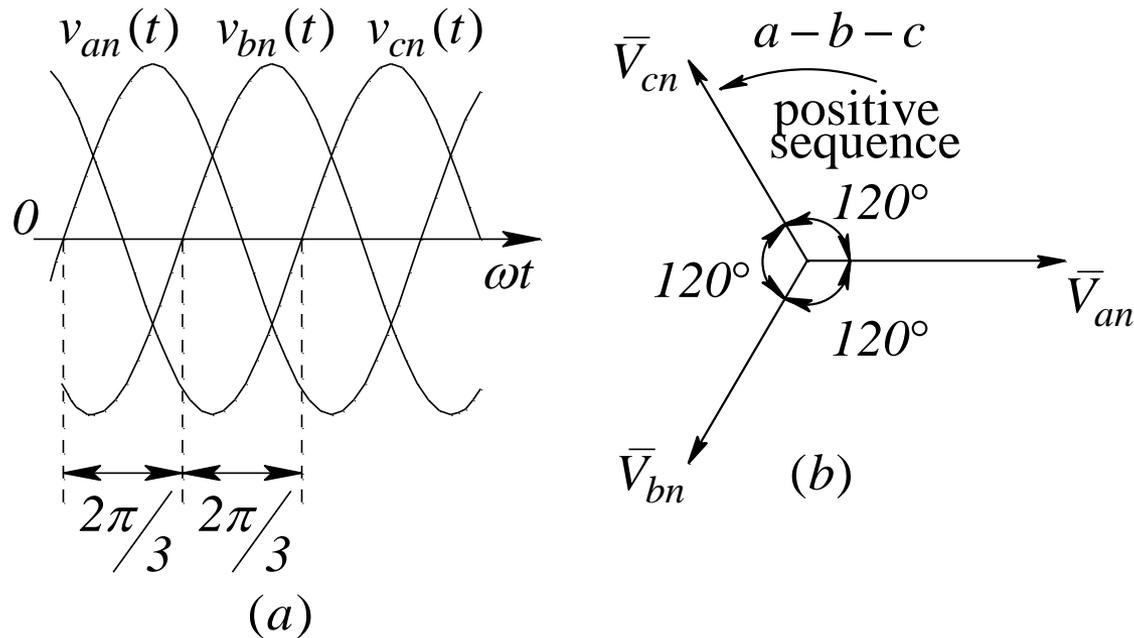


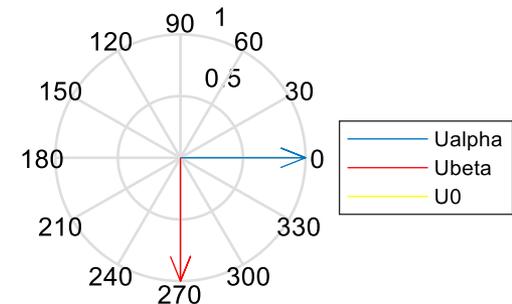
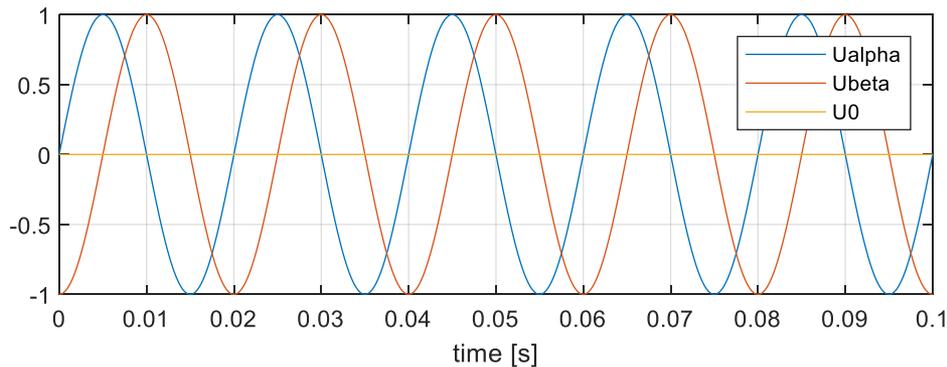
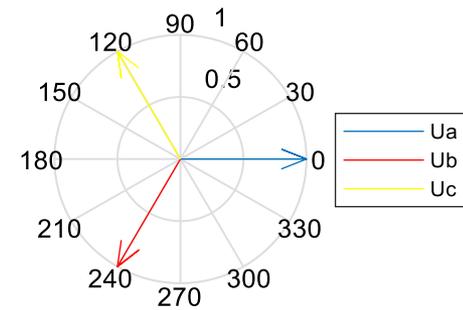
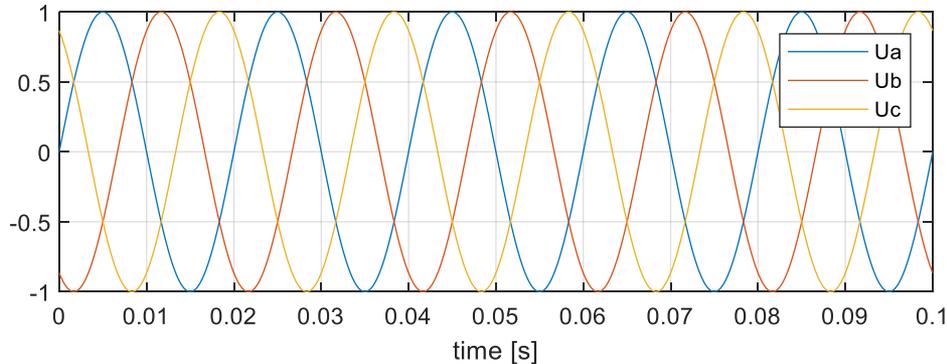
Fig. 2-11 Three-phase voltages in time and phasor domain.

$$\begin{aligned}
 v_{an} &= \sqrt{2}V \cos(\omega t) \\
 v_{bn} &= \sqrt{2}V \cos(\omega t - 120^\circ) \\
 v_{cn} &= \sqrt{2}V \cos(\omega t - 240^\circ)
 \end{aligned}$$

$$\begin{aligned}
 \bar{V}_{an} &= V \angle 0^\circ \\
 \bar{V}_{bn} &= V \angle -120^\circ \\
 \bar{V}_{cn} &= V \angle -240^\circ
 \end{aligned}$$

V is the RMS
phase to neutral
voltage

Transformation 3-ph to 2-ph



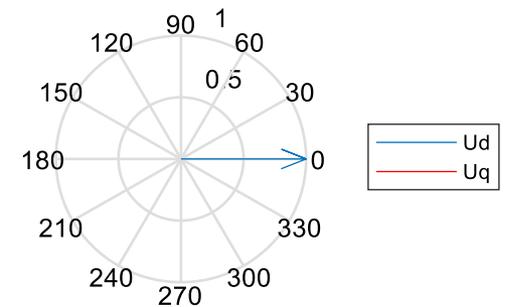
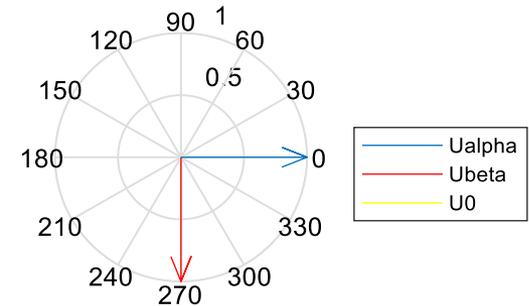
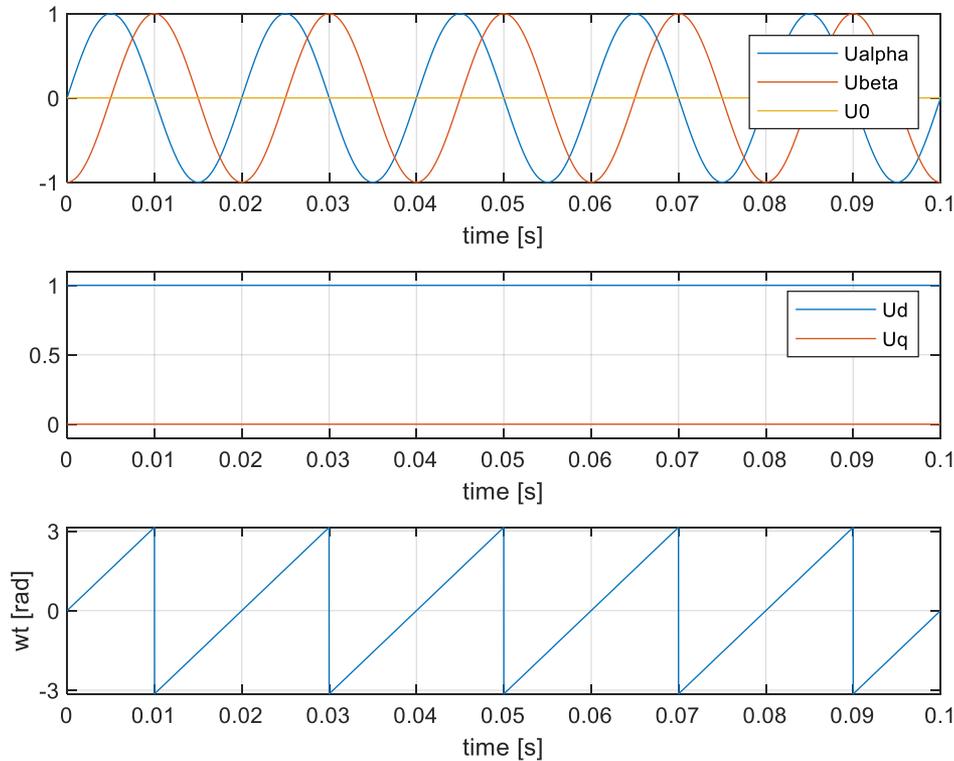
Clarke transform

$$\begin{bmatrix} u_{\alpha} \\ u_{\beta} \\ u_0 \end{bmatrix} = \frac{2}{3} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & -\frac{\sqrt{3}}{2} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix} \begin{bmatrix} u_a \\ u_b \\ u_c \end{bmatrix}$$

$$u_0 = \frac{u_a + u_b + u_c}{3}$$

Transformation to DQ

Transformation to defined synchronous angle reference frame $\theta = \omega t$



Park transform

$$\begin{bmatrix} U_d \\ U_q \\ U_0 \end{bmatrix} = \begin{bmatrix} \sin \omega t & -\cos \omega t & 0 \\ \cos \omega t & \sin \omega t & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u_\alpha \\ u_\beta \\ u_0 \end{bmatrix}$$

DQ transformation, Q: 90deg behind A-axis

alpha/beta to DQ

$$\begin{bmatrix} U_d \\ U_q \\ U_0 \end{bmatrix} = \begin{bmatrix} \sin \omega t & -\cos \omega t & 0 \\ \cos \omega t & \sin \omega t & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u_\alpha \\ u_\beta \\ u_0 \end{bmatrix}$$

abc to DQ

$$\begin{bmatrix} U_d \\ U_q \\ U_0 \end{bmatrix} = \frac{2}{3} \begin{bmatrix} \sin(\omega t) & \sin\left(\omega t - \frac{2\pi}{3}\right) & \sin\left(\omega t + \frac{2\pi}{3}\right) \\ \cos(\omega t) & \cos\left(\omega t - \frac{2\pi}{3}\right) & \cos\left(\omega t + \frac{2\pi}{3}\right) \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix} \begin{bmatrix} u_a \\ u_b \\ u_c \end{bmatrix}$$

$$\begin{bmatrix} u_a \\ u_b \\ u_c \end{bmatrix} = \begin{bmatrix} \sin(\omega t) \\ \sin\left(\omega t - \frac{2\pi}{3}\right) \\ \sin\left(\omega t + \frac{2\pi}{3}\right) \end{bmatrix}$$

abc to DQ



$$\begin{bmatrix} u_d \\ u_q \\ u_0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

DQ transformation, Q: Aligned with A-axis

alpha/beta to DQ

$$\begin{bmatrix} U_d \\ U_q \\ U_0 \end{bmatrix} = \begin{bmatrix} \cos \omega t & \sin \omega t & 0 \\ -\sin \omega t & \cos \omega t & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u_\alpha \\ u_\beta \\ u_0 \end{bmatrix}$$

abc to DQ

$$\begin{bmatrix} U_d \\ U_q \\ U_0 \end{bmatrix} = \frac{2}{3} \begin{bmatrix} \cos(\omega t) & \cos\left(\omega t - \frac{2\pi}{3}\right) & \cos\left(\omega t + \frac{2\pi}{3}\right) \\ -\sin(\omega t) & -\sin\left(\omega t - \frac{2\pi}{3}\right) & -\sin\left(\omega t + \frac{2\pi}{3}\right) \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{2} \end{bmatrix} \begin{bmatrix} u_a \\ u_b \\ u_c \end{bmatrix}$$

$$\begin{bmatrix} u_a \\ u_b \\ u_c \end{bmatrix} = \begin{bmatrix} \sin(\omega t) \\ \sin\left(\omega t - \frac{2\pi}{3}\right) \\ \sin\left(\omega t + \frac{2\pi}{3}\right) \end{bmatrix}$$

abc to DQ



$$\begin{bmatrix} u_d \\ u_q \\ u_0 \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix}$$

Phase synchronization

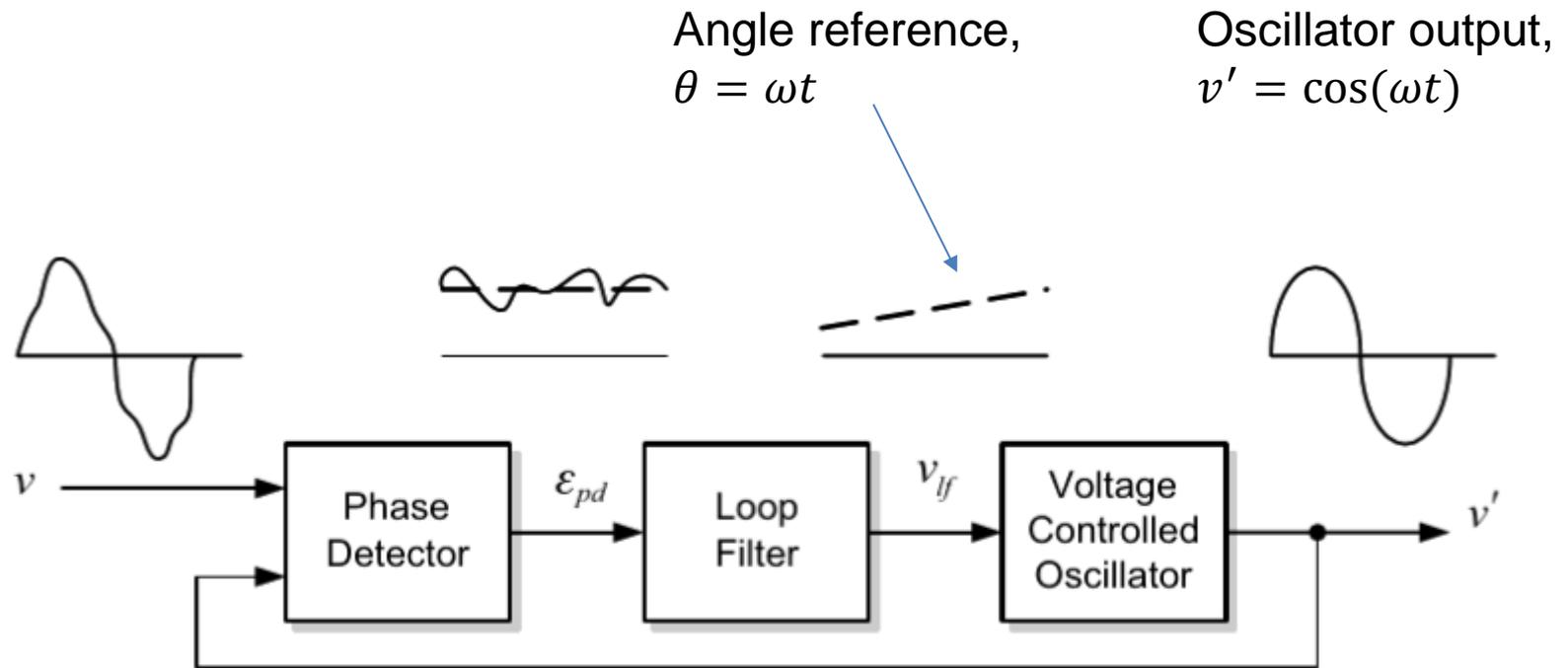


Figure 4.4 Basic structure of a PLL

Phase Locked Loop

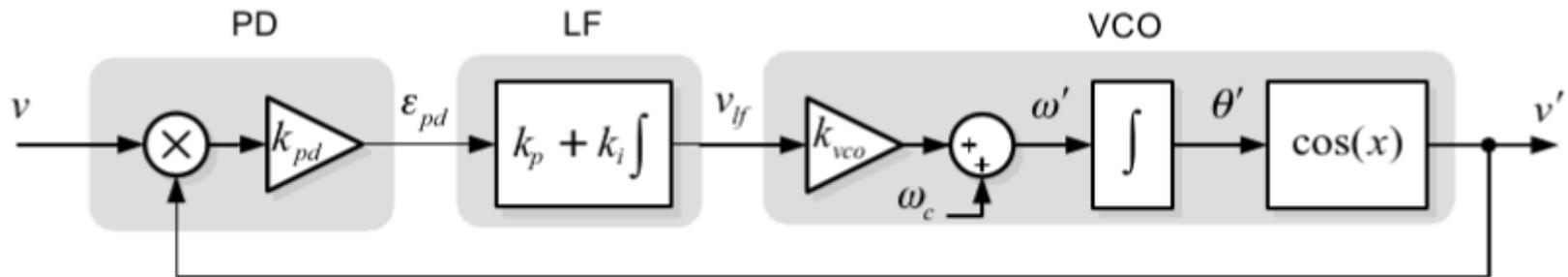
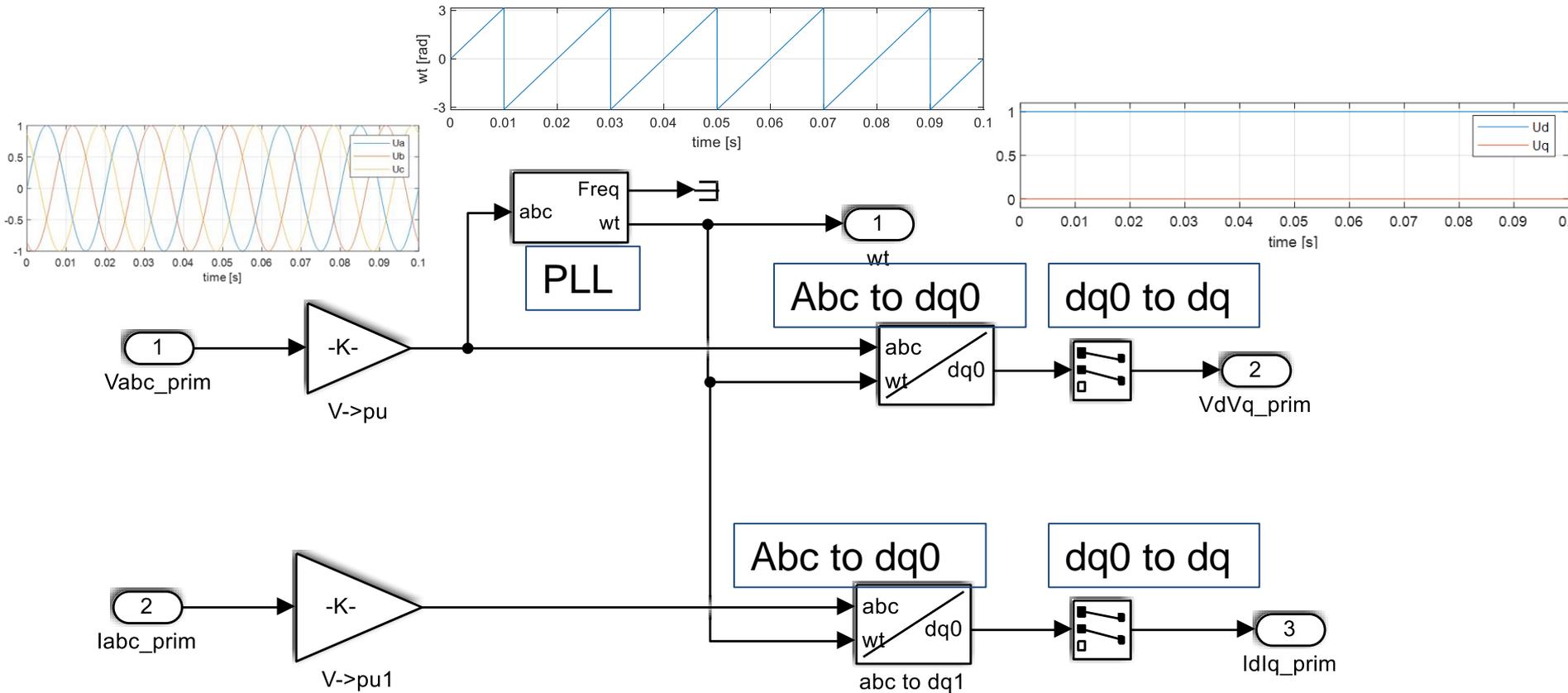


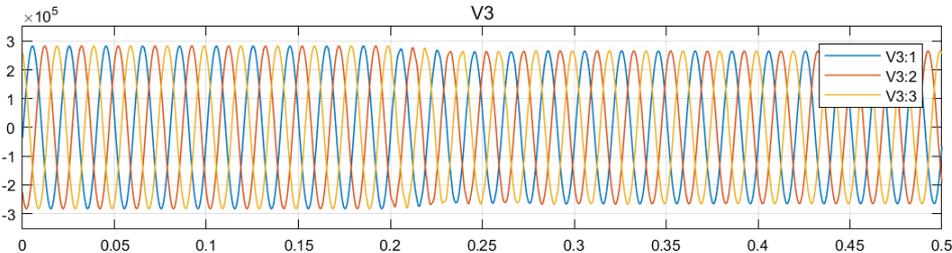
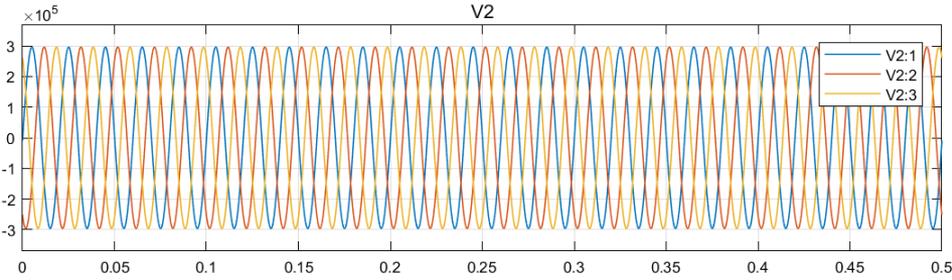
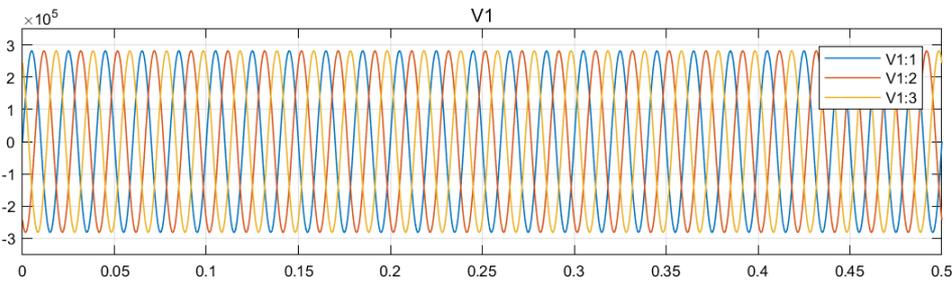
Figure 4.5 Block diagram of an elementary PLL

PI control of error $\varepsilon_{pd} = 0$
Makes v and v' in phase

PLL and coordinate transform of grid voltage and current

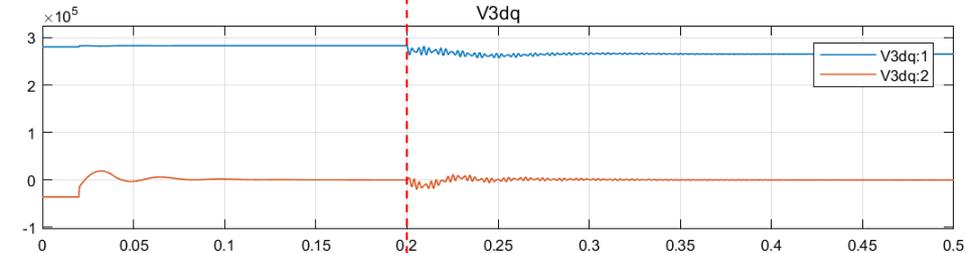
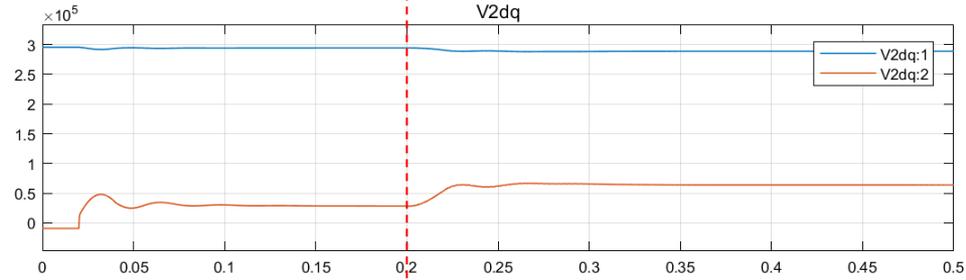
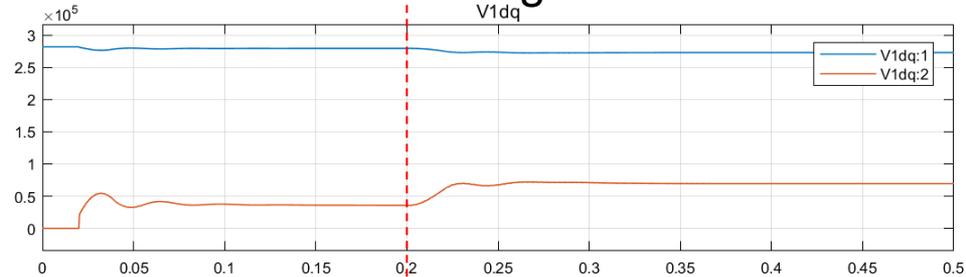


PLL to define DQ-frame



PLL synchronized to V3

Load change

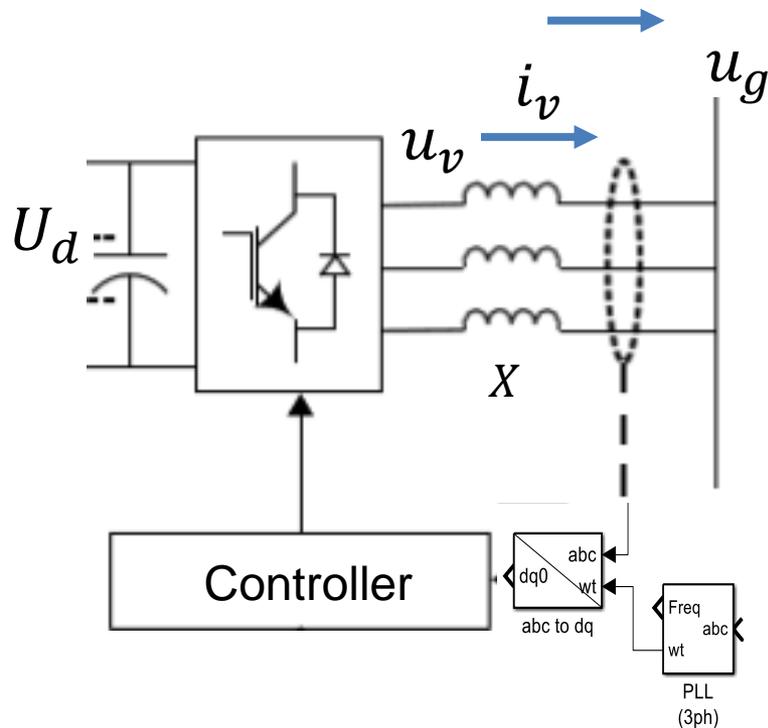


PLL
synch
time

PLL
synch
time

Current control in dq-frame

$$P_g + jQ_g = 3 \cdot u_g \cdot i_v$$



- u_v is controlled to achieve $i_v = i_{vRef}$
- u_g and i_v are measured
- $\bar{U}_{vDQref} = \bar{U}_{gDQ} + j\omega L \bar{I}_{vDQ}$
 - Individual phase control not needed
 - PI-control possible due to dc reference
 - $i_{vRef} = \hat{I}_{vDRef} + j \hat{I}_{vQRef}$
 - P_g and Q_g independently controlled through I_{vd} and I_{vq}

Vector control

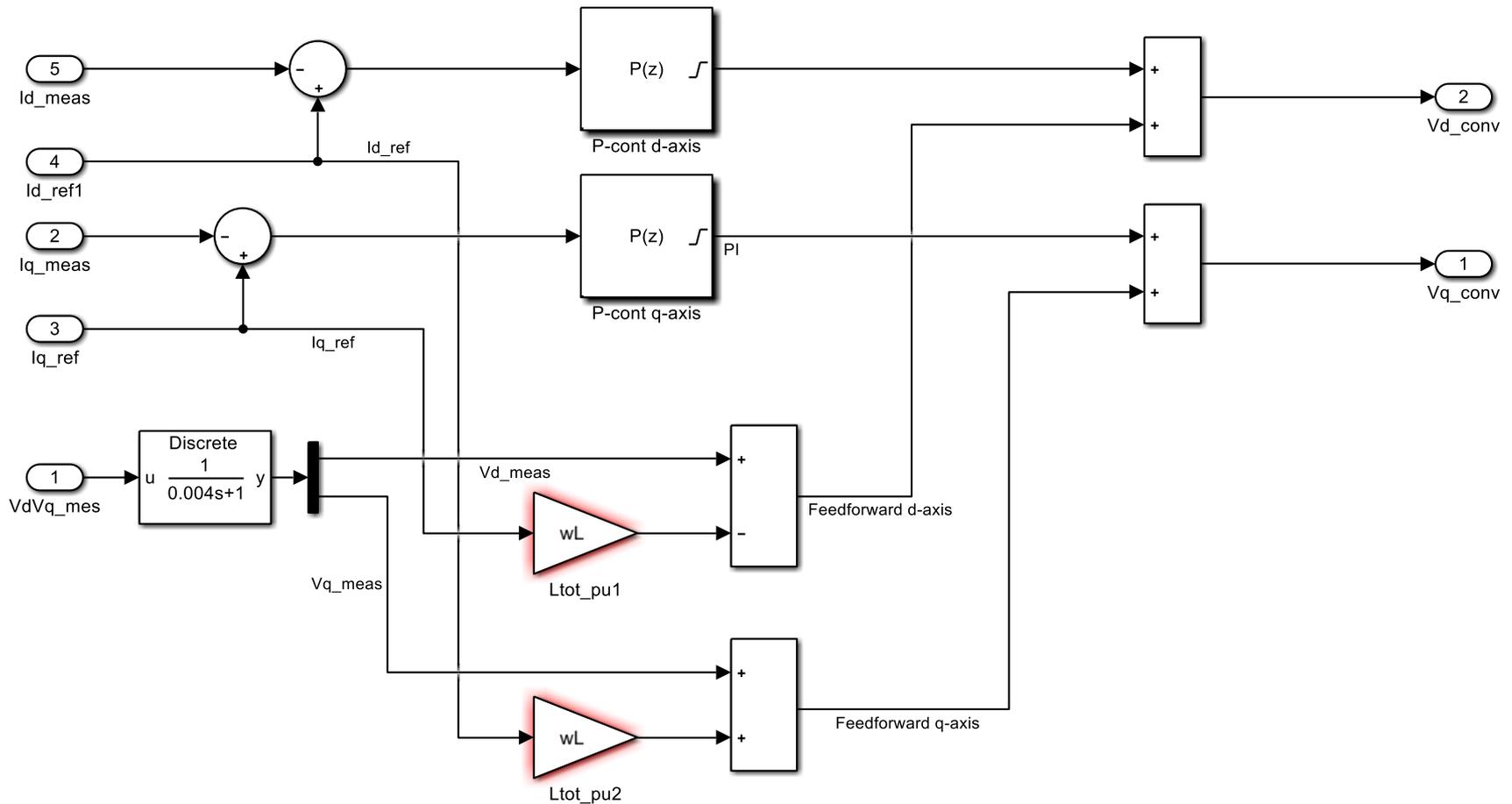
$$P_g + jQ_g = \sqrt{3} \cdot U_g \cdot I_v^*$$

- Control current in DQ-frame: I_{vd}, I_{vq}
- Based on grid voltage: U_{gd}, U_{gq}
- PLL synchronized to U_g makes $U_{gq} = 0$
- $$P_g + jQ_g = \frac{3}{2} (U_{gd} + jU_{gq}) \cdot \text{conj}(I_{vd} + jI_{vq})$$
$$= \frac{3}{2} U_{gd} (I_{vd} - jI_{vq})$$

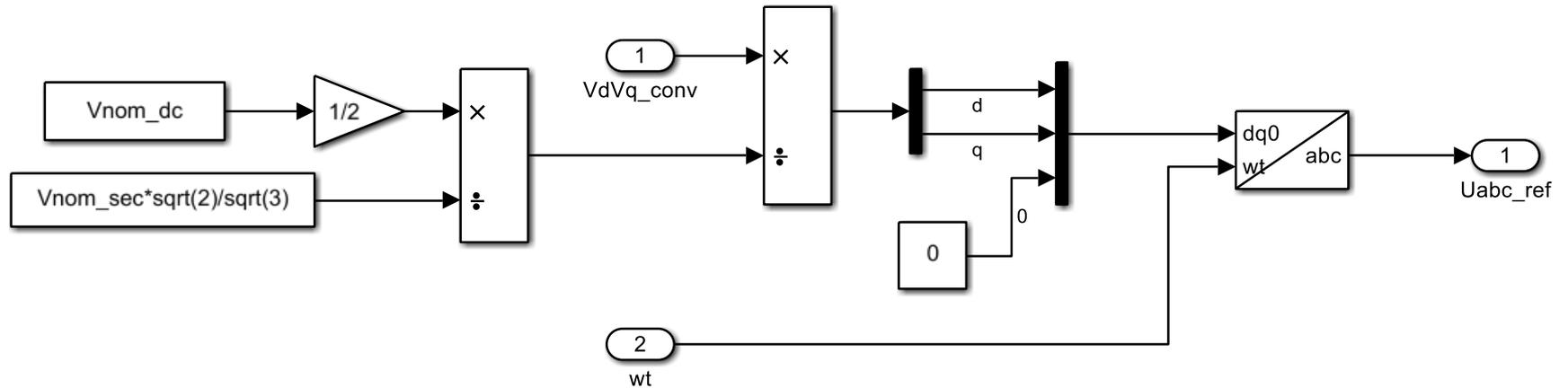
Vector control, ...

- $\bar{U}_v = \bar{U}_g + j\omega L\bar{I}_v$ (Here \bar{U}_v and \bar{U}_g are ph-gnd voltages)
- \bar{I}_{vDQ} , transform from ABC to DQ
- $\bar{U}_{vDQref} = \bar{U}_{gDQ} + j\omega L\bar{I}_{vDQref} + \underbrace{k(\bar{I}_{vDQ} - \bar{I}_{vDQref})}_{\text{proportional control}}$
- PLL (Phase Locked Loop) required to define ωt

DQ current controller



Vd/Vq to Uabc

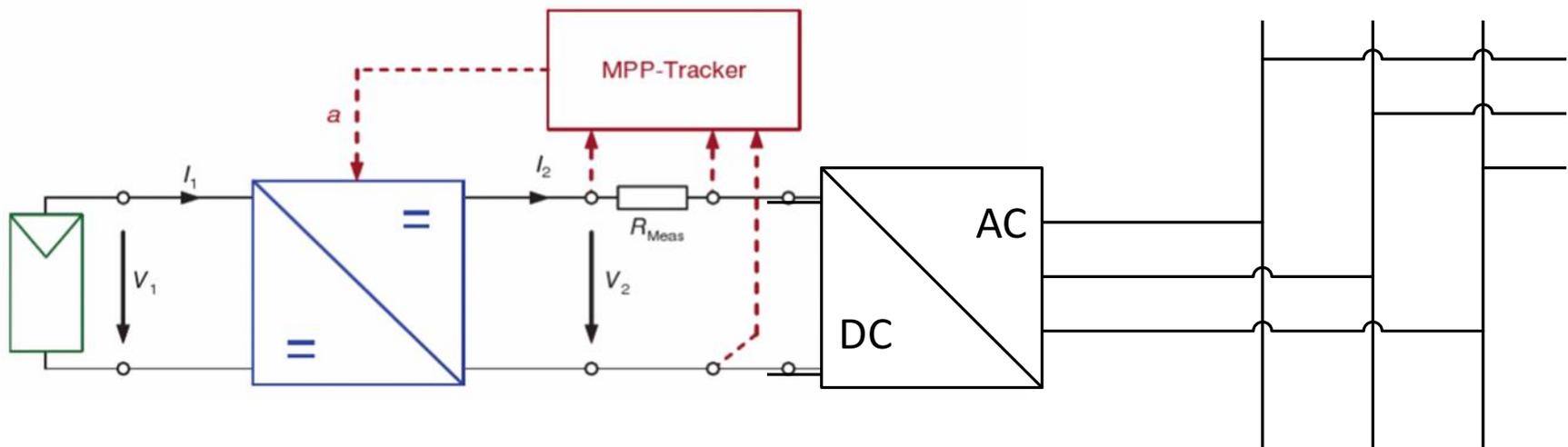


$$U_v = \sqrt{\frac{3}{2}} \cdot m_a \frac{U_d}{2}$$

$$m_a = \frac{U_v \sqrt{\frac{2}{3}}}{\frac{U_d}{2}}$$

PV-system MPPT for grid infeed

- DC/DC conversion
 - to increase voltage from PV to inverter
 - to optimize PV-panel voltage, V_1 , for maximum power
- DC/AC inverter for grid connection
 - Reactive power grid support
 - DC voltage V_2 control



MPPT, Maximum Power Point Tracking

- DC/DC converter to allow different pv- and load voltage
- PV-voltage is optimized to reach MPP

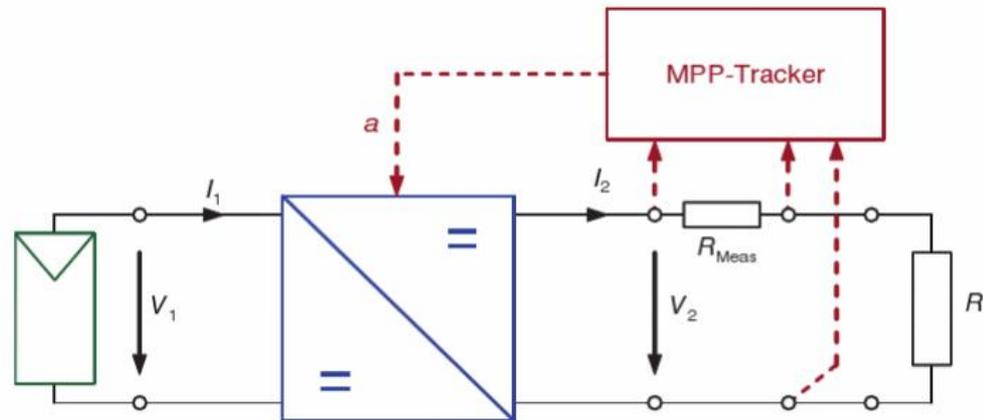
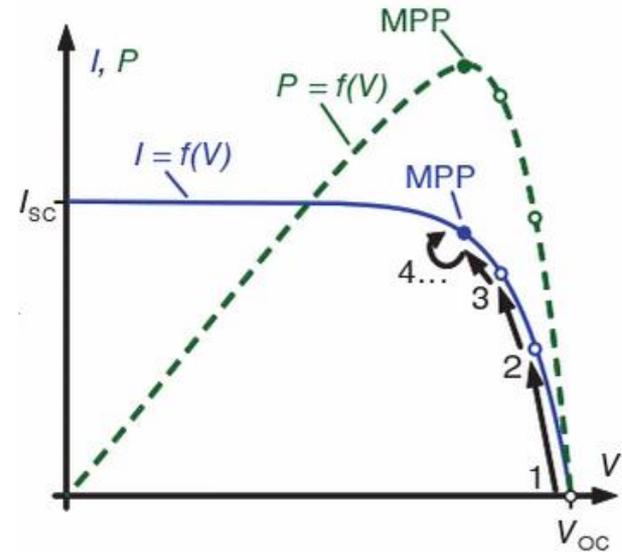
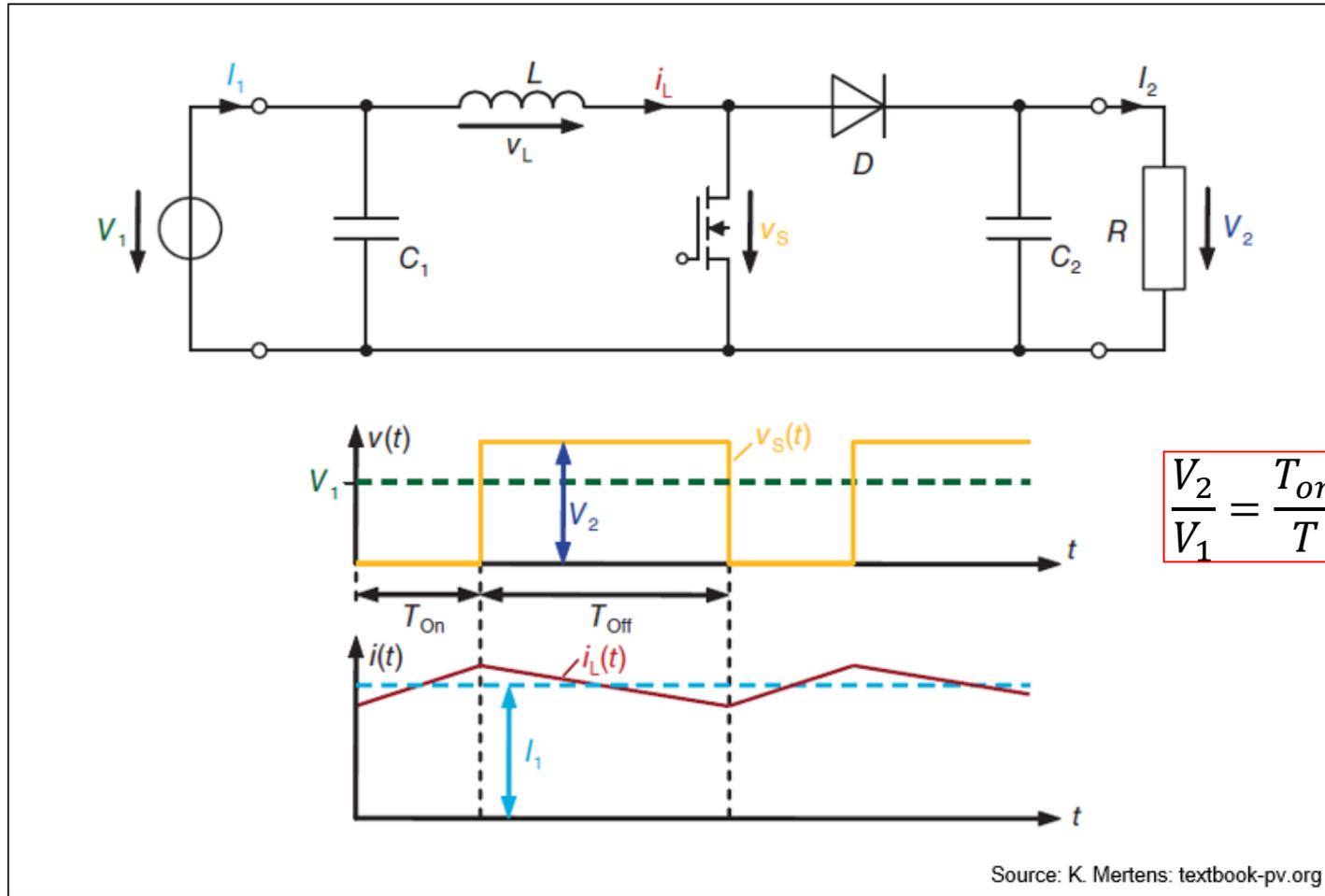


Figure 7.6 Principle of MPP tracking: The output power is maximized by measuring the current and voltage with the simultaneous variation of the duty factor

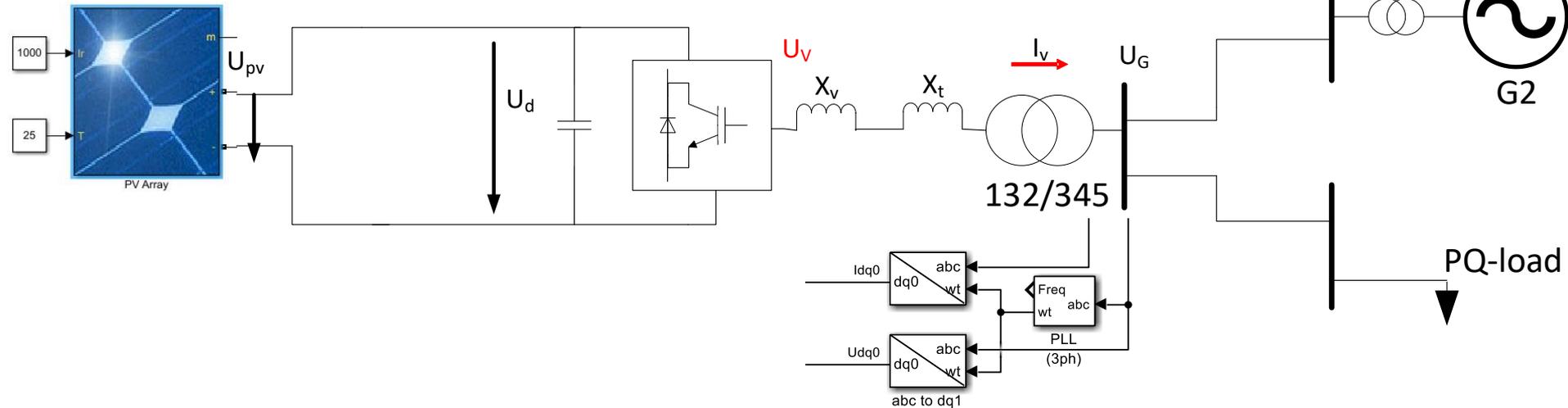
DC/DC step-up(boost) converter



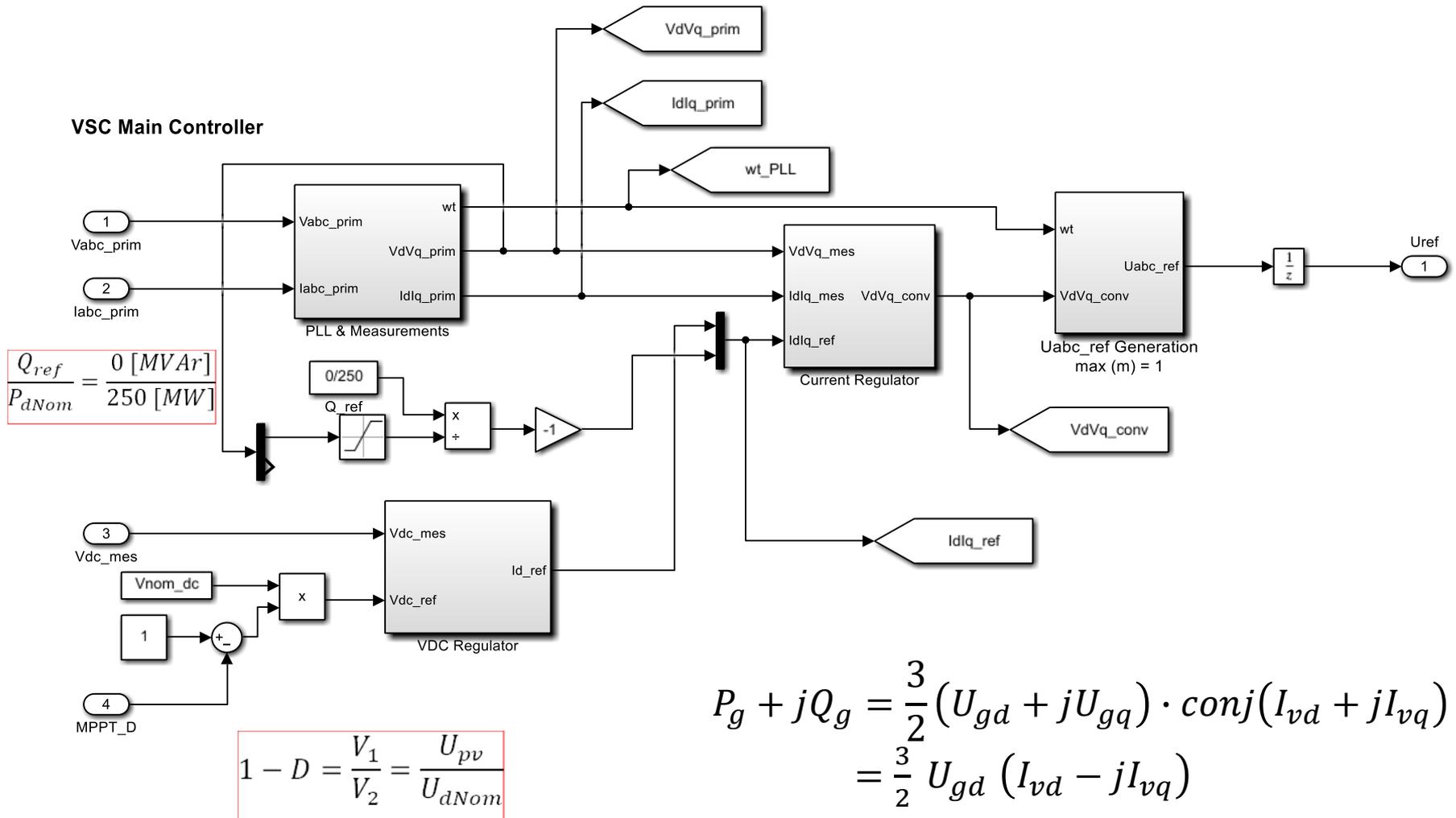
PV-system MPPT for grid infeed

- DC/DC not needed when PV output voltage is high enough
- DC/AC inverter for grid connection
 - Reactive power grid support
 - DC voltage control for MPPT

$$U_v = \sqrt{\frac{3}{2}} \cdot m_a \frac{U_d}{2}$$

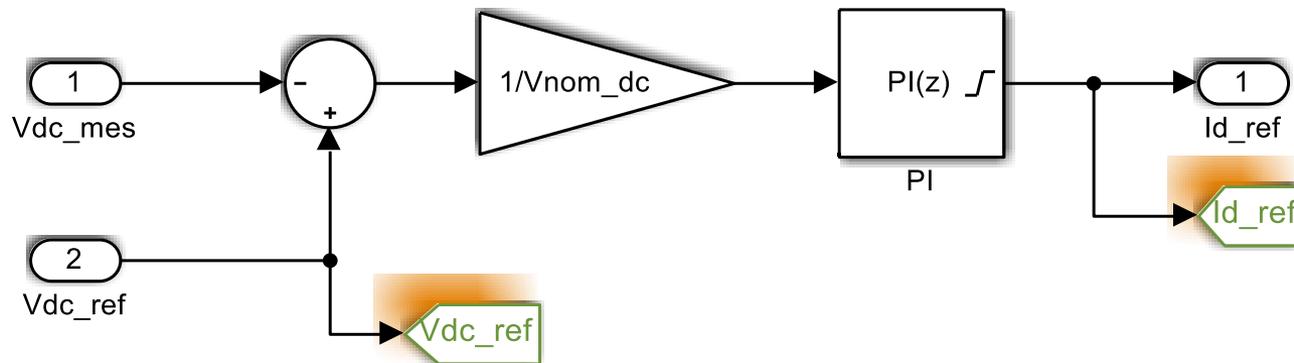


Inverter control



DC/AC grid inverter control

- DC voltage control to define \bar{I}_{vDref}



- Reactive defined by \bar{I}_{vQref}

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